1. Introduction

In recent years, body-centric communications, by which wireless networks are composed between wearable devices, have become an active area of research because of their various applications such as e-healthcare, security systems, and personal services [1]–[11]. The body-centric communications using electric field below several megahertz around the human body are also known as intra-body communications. The physical channels of the intra-body communications have been treated as a capacitive circuit from the beginning of the development. Although the circuit-like understanding of the channels are helpful to design devices and systems, there is a problem that the results may be invalid if the circuit parameters are incorrectly estimated. In the present study, the values of the circuit parameters are properly derived by solving a boundary value problem of electric potentials of the conductors. Furthermore, approximate models which are appropriate for cases that some of the conductors are grounded are investigated.

**SUMMARY**

Physical channels of the intra-body communications, in which communications are performed by exciting electric field around the human body, have been treated as a capacitive circuit from the beginning of the development. Although the circuit-like understanding of the channels are helpful to design devices and systems, there is a problem that the results may be invalid if the circuit parameters are incorrectly estimated. In the present study, the values of the circuit parameters are properly derived by solving a boundary value problem of electric potentials of the conductors. Furthermore, approximate models which are appropriate for cases that some of the conductors are grounded are investigated.

**key words:** intra-body communications, quasi-static approximation, equivalent circuit, boundary value problem

2. Procedure to Derive the Equivalent Circuit

First of all, we describe the procedure to express the general problem of conductor systems as an equivalent circuit. As an example, in a case that three conductors are in free space as shown in Fig. 1(a), the potentials and the net charges of respective conductors have a linear relationship as below.

\[
\begin{pmatrix}
\phi_1 \\
\phi_2 \\
\phi_3
\end{pmatrix} =
\begin{pmatrix}
c_{11} & c_{12} & c_{13} \\
c_{21} & c_{22} & c_{23} \\
c_{31} & c_{32} & c_{33}
\end{pmatrix}
\begin{pmatrix}
q_1 \\
q_2 \\
q_3
\end{pmatrix}
\]

(1)

where, \(c_{ij}\) is the capacitance coefficient, \(\phi_j\) is the potential
of each conductor, and \( q_i \) is the net charge. Each capacitance coefficient can be obtained by solving a boundary value problem of electric potentials of the conductors. For example, by obtaining the charge distributions of each conductor under a condition of \( \phi = (1, 0, 0)^T \), we can find the values as \( c_{11} = q_1 \), \( c_{21} = q_2 \), and \( c_{31} = q_3 \). The potentials of each conductor in arbitrary net charge conditions can be obtained by solving Eq. (1) in which the charge vector in the right hand is specified.

Figure 1(b) shows the equivalent circuit corresponding to the conductor system. This circuit is a network of which all nodes including the infinite distance of reference potential \( V = 0 \) are connected with capacitors. The nodal equation of the circuit is as follows.

\[
\begin{align*}
\sum_j & \left( C_1 + C_{12} + C_{13} - C_{12} - C_{13} 
\begin{array}{c}
- C_{12} \\
- C_{13} \\
- C_{23}
\end{array}
\right) \begin{array}{c}
V_1 \\
V_2 \\
V_3
\end{array} = \\
\begin{array}{c}
I_1 \\
I_2 \\
I_3
\end{array}
\end{align*}
\]

where, \( V_j \) is the potential of each node, \( I_j \) is the current flowing into each node. Considering the relationship of \( I = jwQ \) between current \( I \) and charge \( Q \), we find that the relationship of Eq. (2) is essentially equal to that of Eq. (1). Hence, by comparing these matrices, the equivalent-circuit parameters can be formally obtained as \( C_1 = c_{11} + c_{12} + c_{13} \), \( C_{12} = -c_{12} \), and \( C_{13} = -c_{13} \).

3. Model and Numerical Methods for Investigation

Figure 2 shows the structure of the model for the present investigation. For simplicity, the human body is modeled by a perfect conducting sphere. Its diameter is 300 mm which corresponds to the longest diameter of the human torso [12]. The transmitter and the receiver have a same structure of which two electrodes are 30 mm in side length and separated each other by a gap of 5 mm. These dimensions are small enough both for on- and off-body applications. Both of the transmitter and the receiver are equipped on the conducting sphere with a 5-mm separation from the sphere, assuming some covers and clothes. The angle \( \theta \) formed between the transmitter and the receiver is varied from 20° to 180°. Incidentally, since the actual human body has some amount of resistance, the voltage drop and the loss due to conducting currents inside the body are expected to get larger as the frequency increases. Regarding to this, we have already conducted some additional tests and confirmed that the discrepancy of received voltage from the static approximation is at most 3 dB in a range below 60 MHz. The detail is described in the Appendix.

The static characteristics of the model were numerically analyzed by using the method of moment (MoM) based on the potential integral equation and the Galerkin’s method [13]. The electrodes are divided into rectangular constant elements which have unit net charge. The ratio of the mesh sizes is equal to that of weight factors for the Gaussian quadrature [14]; that is, the meshes neighboring the edges have the minimum size. Division number of each electrode is 32 × 32. Instead of dividing the sphere into elements, we used a Green’s function of which value is zero on the surface of the sphere. This Green’s function is based on the image charge method [15], and transformed to a reciprocal form between the source and observation points as follows.

\[
G(r, r') = \frac{1}{|r-r'|} - \frac{1}{\sqrt{|r|^2|r'|^2/a^2 - 2r \cdot r' + a^2}}
\]

where, \( r \) is the observation point, \( r' \) is the source point, and \( a \) is the radius of the sphere. If the given potential on the sphere \( \phi_{\text{sphere}} \) is not zero, a point charge can be assumed at the center of the sphere so as to satisfy the given boundary condition. Therefore, the integral equation to be solved is as follows.

\[
\phi(r) - \frac{a}{|r|} \phi_{\text{sphere}} = \frac{1}{4\pi\varepsilon_0} \int_S G(r, r')\sigma(r')dS'
\]

where, the second term of the left hand is the contribution of the point charge, \( \varepsilon_0 \) is the permittivity of vacuum, \( \sigma \) is the surface charge on the electrodes, and \( S \) is the surface region of the electrodes.
In order to validate the MoM analysis described above, we also employed the FDTD method. The dimensions of the computational domain are $600 \text{ mm} \times 600 \text{ mm} \times 600 \text{ mm}$; and 20-layer perfectly matched layer (PML) surrounds the domain. The cell sizes in a region including the electrodes and the sphere are $\Delta x = \Delta y = \Delta z = 1 \text{ mm}$. The sphere is approximated by using the staircasing. The maximum cell size neighboring the PML absorbing boundary is 5 mm. The transmitter is fed at the central point of the electrodes by a current source with uniform current distributions and infinite internal impedance. The exciting waveform is the derivative Gaussian pulse, of which spectrum is $-60 \text{ dB}$ at 1 GHz. Since the feeding charge is a time integral of the feeding current, the charge has a waveform of the Gaussian pulse; therefore, the spectrum of the charge has maximum value at zero frequency. The top and bottom electrodes of the receiver are open ended in order to obtain open voltages by a line integral of the electric field.

As well as in the MoM analysis, the static characteristics should be obtained in this FDTD analysis. In the present case, the number of the PML layers is large enough so that its precision is ensured for relatively-low frequency [16]. Thus, the convergence of the field of interest is faster than the risetime of the undesired reflections from corners of outer boundaries. For this reason, by terminating the iterative updates of electromagnetic field and the Fourier transform immediately after the convergence of field, the static characteristics can be obtained with acceptable accuracy. The duration of the fielded calculation is about $19.2-57.6 \text{ ns}$, depending on cases. The time of the convergence were confirmed by once observing the long-duration transient field at a corner of the domain. Then, the field distributions were calculated again in a shorter duration appropriate for each case. Incidentally, if the number of the PML layers is not enough, the risetime of the undesired reflections is much faster, and so they are unable to be excluded. Likewise, if the maximum frequency of the exciting pulse is too lower, the time for the convergence is much longer; therefore, the field of interest is unable to be separated with the reflections. We have figured out enough values for the pulse waveform and the PML layers through trial-and-error processes.

4. Parameters of Equivalent Circuit and Signal Transmission Characteristics

Figure 3 plots the equivalent-circuit parameters calculated by the MoM. The solid lines indicate the capacitances between the electrodes of one device and the body (Bot.–Body, Top–Bot., and Top–Body); the broken lines indicate the capacitances of each conductor with the infinite distance (Body–Inf., Top–Inf., and Bot.–Inf.); and the chained line indicate the capacitances between respective electrodes of the transmitter and the receiver (Top–Top’, Top–Bot’, and Bot.–Bot’: Tx–Rx couplings). In addition, specific values of the parameters at $\theta = 90^\circ$ and $180^\circ$ are listed in Table 1. Naturally, the direct couplings between the transmitter and the receiver depend on the receiver position $\theta$; and their values are relatively small compared with the others. By contrast, the other parameters hardly depend on $\theta$; and the largest one is the capacitance of the body with the infinite distance (Body–Inf.), followed by that between each conductor (Bot.–Body, Top–Bot., and Top–Body), and that of each electrode with the infinite distance (Top–Inf. and Bot.–Inf.). The large amount of the capacitance of the body with the infinite distance is due to the large dimension of the body.

Figure 4 plots the received voltages in various conditions. Here the received voltages are normalized by the input voltage. In the case that no conductor is grounded (No grounding: this case corresponds to some on-body applications such as sensing of biological information and head mount displays [1], [3]), the received voltage decreases with
increasing $\theta$. This fact indicates that the direct couplings between the transmitter and the receiver are not negligible even though their values are relatively small; and accordingly, the equipping position of devices and user’s postures are important for the on-body applications. At large $\theta$ more than about 120°, however, the received voltage almost converges; that is, contribution of the direct couplings becomes relatively small. By contrast, when the body is grounded (Grounding body), the received voltage does not converge even at large $\theta$. This is due to a fact that the coupling through the infinite distance is not available because the body and the infinite distance are equal in potential as also described in [4]. In the cases that the top electrode of one device is grounded (Grounding Tx and Grounding Rx), the value and the stability of the received voltage are considerably improved. This is because the coupling through the infinite distance is dominant. These results suggest that the equipping position of devices is not so important in the off-body applications. Furthermore, when the both devices are grounded, the performance is better than the previous cases. Incidentally, the symbols plotted in Fig. 4 indicate the results by the FDTD method. In order to ground some conductors, thin conducting wires are connected with them and extended into inside of the PML. Therefore, the models for the FDTD and the MoM are not exactly the same; however, the calculated values almost agree with each other. Hence, the numerical analyses conducted here are most likely valid.

In addition, in order to understand the phenomenon from electromagnetic view, Figs. 5(a)–(e) shows the electric field distributions on the plane of $y = 0$ when $\theta = 180^\circ$ in respective cases. In all the cases, the distributions by the MoM and the FDTD agree with each other, as well as in Fig. 4. Comparing (b) to (a), the distributions around the transmitter (top side of the sphere) are almost the same as that in (a), but attenuate more rapidly. That is because the electric charges which contribute to the electric field around the bottom side in (a) have gone away to the infinite distance (or the earth ground).

Regarding (c), the distributions are almost uniform around the surface of the sphere. This corresponds to the stability of the received voltage in Fig. 4, and is because the absolute value of the potential of the sphere (contributed by the point charge assumed at the center of the sphere) is larger than that in (a). On the other hand, the distributions in (d) are not uniform as in (c). But since the potential should be constant on the sphere and that of the grounded electrode is forced to be zero, the potential difference between them is also constant; therefore, almost uniform electric field is supposed to be generated between them. Actually, as shown in (d), the electric field in a region between the body and the grounded electrode seems to be enhanced. In another respect, this is contributed by charges supplied from the infinite distance to the grounded electrodes. This is the alternative proof that the received voltage is stable when the receiver is grounded.

### 5. Investigations of Approximate Circuit Models

In this section, we select negligible parameters out in each case considered in the previous section, and investigate what approximate models are reasonable.

#### 5.1 Case 1: No Conductor is Grounded

In order to figure important parameters out first, Fig. 6 plots the received voltages with omitting some parameters in the case that no conductor is grounded. First, the received voltage with omitting the direct couplings between the transmitter and the receiver is quite different from the exact one as already suggested in the previous section (Omit. Tx–Rx). But another result with omitting the direct coupling only between the bottom electrodes agrees with the exact result (Omit. Bot.–Bot.’); and furthermore, even if only the direct coupling between the top electrodes is taken into account, the result largely agrees with the exact one (Omit. Tx–Rx except Top–Top’).
Fig. 6  Received voltages with omitting some parameters when no conductor grounded.

Fig. 7  Approximate model when no conductor is grounded.

Regarding other parameters, in the case that the coupling between each top electrode and the human body is omitted, the estimated received voltage is almost 10 dB higher than the exact one (Omit. Top–Body); therefore, it is not omissible. Finally, the result with omitting the coupling between each bottom electrode and the infinite distance has a little discrepancy with the exact one at larger $\theta$ (Omit. Bot.–Inf.); but the amount is less than 1.4 dB. Considering these results, it is concluded that at least parameters shown in Fig. 7 should be taken into account. The model in Fig. 7 is much more complicated than any other approximate models proposed previously. In addition, we would like to note again that the direct coupling between the transmitter and the receiver is significant in the on-body applications and the equipping position and user’s posture should be taken into account.

5.2 Case 2: The Body is Grounded

Next, we discuss the case that the human body is grounded. In this case, the human body and the infinite distance are equal in potential; therefore, capacitances of each electrode with the reference potential are the sum of those with the human body and with the infinite distance. Since the capacitances with the human body are sufficiently larger than those with the infinite distance, the capacitances of each conductor with the infinite distance are expected to be omissible. Figure 8 plots the received voltages with omitting some parameters. In the case that the capacitance of the bottom electrodes with the infinite distance and that between each bottom electrode, the result almost agrees with the exact one (Omit. Bot.–Inf. & Bot.–Bot.). On the other hand, the result with omitting capacitances of each top electrode with the infinite distance do not exactly agree with the exact one (Omit. Top–Inf.). However, the discrepancy is less than 1.1 dB; therefore, they are most likely omissible. In addition, in the case that the direct couplings between the transmitter and the receiver except between the top electrodes are omitted, the discrepancy is somewhat larger (1.7 dB) than that in the ungrounded case. According to these results, the approximate circuit model for this case is as shown in Fig. 9.

5.3 Case 3: Devices are Grounded

Finally, we consider the cases that either or both of the transmitter and the receiver are grounded. If one device is grounded, the capacitances between the electrodes of other device and the reference potential are the sum of those with the grounded electrode and with the infinite distance. Since the direct couplings between the transmitter and the re-
receiver are relatively small, they are omissible. Therefore, the received voltage is supposed to be independent with the equipping position of devices. Similarly, some couplings with grounded electrodes are expected to be omissible. Figures 10–12 plot the received voltages with omitting some parameters in the respective cases. The common point is that the direct couplings between the devices are almost omissible as expected (plotted with solid lines). In addition, the results indicate that the coupling between the bottom electrode of grounded device and the infinite distance is also omissible. Furthermore, even if the coupling between the grounded electrode and the human body is omitted, the discrepancy with the exact result is very small. This is also due to the same reason, that is, the capacitance of the body with the grounded electrode is sufficiently small than that with the infinite distance.

Figure 13 shows the approximate model when the transmitter is grounded. This circuit model suggests not only that the channel is independent on the device positions, but also that the potential of the body is sensitive to the capacitance between the bottom electrode of the transmitter and the body. In other words, the received voltage strongly depends on the distance between the transmitter and the body. Therefore, it may be suggested that an action touching the off-body transmitter can be used as a trigger for communications. In addition, the approximate model when the receiver is grounded have a composition that the transmitter and the receiver are interchanged in Fig. 13.

Finally, Fig. 14 shows the approximate circuit model for the case that both of the transmitter and the receiver are grounded. This model is relatively similar to models pro-
Posed in some previous studies [7]. Of course, if we measure the channel with a network analyzer, the channel should behave as Fig. 14. Therefore, if we need to assess the channels for on-body applications, the devices should be isolated from the ground of the instruments.

5.4 Received Voltages by Using Approximate Models

In order to examine the validity of the approximate models described in previous subsections, Fig. 15 compares the received voltages calculated by using the approximate models with the exact values. In all the cases, the discrepancies are less than 2 dB in a range of $\theta \geq 40^\circ$. Hence, the approximate models proposed here are most likely enough to grasp the behavior of the channel.

6. Conclusion

In the present study, the equivalent-circuit expressions of the intra-body communications channels using the quasi-static field were properly derived by solving a boundary value problem of electric potentials of the electrodes and the human body. Then, the signal transmission characteristics in various conditions were calculated with the obtained circuit parameters. According to the results, in the case that either or both of the transmitter and the receiver are grounded, the value and the stability of the received voltage are improved because the coupling through the infinite distance becomes dominant.

Furthermore, after we have investigated omissible circuit parameters in each case, it is found that in the case that the devices are not grounded, many parameters, especially the direct couplings between the transmitter and the receiver, are not negligible. Similarly, in the case that the human body is grounded, the most of parameters should be taken into account. We believe that these facts are important in considering on-body applications such as e-healthcare and personal services. By contrast, if either of the transmitter and the receiver is grounded, the direct couplings between them are negligible. This fact is most likely important for off-body applications such as personal authentication and electronic payment. Especially, in the case that the both devices are grounded, many parameters may be omitted; and therefore, the approximate circuit model is relatively similar to models proposed in some previous studies. Of course, if we measure the channels with a network analyzer, the channel should behave as the last case. Therefore, the devices should be isolated from the ground of the instruments to correctly assess the channels for on-body applications.

In the future, we will consider some effects due to proximity of the earth ground and variations of human posture by employing more realistic human body models.

References

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Appendix: Applicable Frequency of Quasi-Static Approximation

The approximate circuit model in Fig. 14 implies that the received voltage decreases with frequency because the relative amount of impedance of human body increases with frequency. As an example, we assume a lossy circuit model shown in Fig. A·1, which includes a resistance component \( R \) between two points on the human body which face each bottom electrode of the transmitter and the receiver. With this assumption, we find the received voltage \( V_2 \) for input voltage \( V_1 \) as

\[
V_2 = \frac{C_2}{(C_2 + C_3)j\omega C_7 + 1} + \frac{C_5}{C_4 + C_5} V_1 \quad \text{(A·1)}
\]

where, \( C_7 = C_4 C_5/(C_4 + C_5) + C_6 \). Equation (A·1) indicates that \( V_2 \) decreases with increasing \( \omega \). In order to assess the extent of this depression, we have additionally calculated the frequency characteristics of received voltage with a lossy sphere model (\( \epsilon_r = 91.8, \sigma = 0.658 \text{ S/m: muscle at } 30 \text{ MHz} \)) by using the FDTD method.

Figure A·2 plots the frequency dependence of the received voltages in respective cases. Here the position of the receiver is \( \theta = 180^\circ \). At zero frequency, the voltages almost agree with that in Fig. 4 except just a little numerical error. As implied by Eq. (A·1), the received voltage when both devices are grounded decreases with increasing frequency. However, the depression is within 3 dB below 60 MHz. In addition, the received voltage with the grounded body approaches to that with the ungrounded body as the frequency increases. This is due to a fact that it takes relatively long time before the excited electromagnetic waves have propagated to the infinite distance through around the body and the grounding wire.

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