Biological Tissue-Equivalent Agar-Based Solid Phantoms and SAR Estimation Using the Thermographic Method in the Range of 3–6 GHz

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SUMMARY In this paper, the electrical constants of a biological tissue-equivalent agar-based solid phantom from 3.0 to 6.0 GHz are described. The developed phantom can reproduce the electrical constants of biological tissues from 3.0 to 6.0 GHz, and it is not necessary to change the phantom for each frequency band in the range of 3.0 to 6.0 GHz during the measurements. Moreover, adjustments to the dielectric constants of the phantom at 3.0, 3.8, 5.2, and 5.8 GHz are presented. The constants of this phantom can be adjusted mainly by using polyethylene powder and sodium chloride. The phantom can be used to evaluate the Specific Absorption Rate (SAR) as well as the antenna characteristics in the range of 3.0 to 6.0 GHz. Furthermore, the effect of the electrical constants of the phantom on the SAR is investigated. The investigation of SAR measurements is performed on the phantom at 5.2 GHz using the thermographic method. Calculations using the FD-TD method and the finite difference method based on the heat conduction equation are carried out in order to evaluate the thermal diffusion in the measurements using the thermographic method. The measured and calculated results are in good agreement. There is evidence that the thermal diffusion influences the SAR estimation at 5.2 GHz more than in a lower frequency range even though this method basically does not depend on the frequency.

key words: solid phantom, broadband, FDTD method, SAR, thermographic method, heat conduction equation

1. Introduction

Many studies on measuring and calculating the Specific Absorption Rate (SAR) at frequencies used in mobile phone systems have been conducted [1]–[3]. The SAR is given by

\[ \text{SAR} = \frac{\sigma E^2}{\rho} \quad [\text{W/kg}] \quad (1) \]

where \( \sigma \) is the electrical conductivity [S/m], \( \rho \) is the density [kg/m\(^3\)], and \( E \) is the electric field [V/m] (r.m.s.).

Recently, frequencies used by wireless LAN devices that are higher than that used by the present cellular systems have become popular and the Ultra Wide Band (UWB) [4] system, which employs a very wide frequency range, was developed. Since these devices may also be used in close proximity to the human body, investigations on the SAR and antenna characteristics while considering human interaction are very important. Additionally, the International Electrotechnical Commission (IEC) has started to develop a SAR measurement method for which the frequency range is expanded to 30 MHz to 6 GHz [5]. It is expected that this method will be used to test these devices operating at a higher frequency range for SAR compliance.

From these points of view, it is also very important to develop a biological tissue-equivalent phantom that has applicable electrical constants at a point and/or broadband characteristics above 3 GHz. Until now, biological tissue-equivalent liquid and solid phantoms have been proposed in order to evaluate the interaction between the human body and an electromagnetic field at frequencies mostly below 3 GHz [5]–[14]. A few recipes for liquid phantoms for frequencies above 3 GHz have been introduced [5], [9]. Since the E-field probe can be easily scanned in liquid, the liquid phantom has been adopted by the SAR measurement method for compliance, e.g. [8]. On the other hand, the solid phantoms proposed in [11]–[13] have also been used for SAR measurement, which is used to measure the E-field or the temperature rise. One of the features of the solid phantom is that it can maintain an arbitrary shape by itself without a shell.

One of our objectives is the development of a biological tissue-equivalent solid phantom, which has broadband characteristics above 3 GHz. In order to achieve this, we focus on a solid phantom based on agar [11], [12], for frequencies above the 3 GHz band. The phantom has been mainly used for dosimetry and evaluating antenna performance in research and development phases. The features of this phantom are its easy adjustment of electrical constants, ease in manufacturing of an arbitrary shape, inexpensive and popular ingredients, and its ability to maintain its shape by itself without a shell. In addition, a heterogeneous phantom can be manufactured.

In this paper, first, adjustments to the electrical constants of the phantom are described from 3 GHz to 5.8 GHz. Then the frequency characteristics of the phantom are described and their broadband characteristics are presented. In addition, we present the results of a study on the effect of varying the phantom constants.

The investigation of SAR measurement on the solid
phantom using the thermographic method [15] above 3 GHz is performed. A numerical study on the combination between the FD-TD method and the finite difference method based on the heat conduction equation [16] in order to evaluate the effect of thermal diffusion is presented.

2. Solid Phantoms

2.1 Biological Tissue-Equivalent Agar-Based Solid Phantoms

Two kinds of biological tissue-equivalent solid phantoms based on agar have been used to evaluate dosimetry as well as antenna characteristics [11],[12]. One of these phantoms is called the TX-151 phantom [11] and the other is called the Glycerin phantom [12]. Each phantom has different features. Compared to the Glycerin phantom, the TX-151 phantom can simulate high-water content organs such as the brain for a wider frequency range below 3 GHz. On the other hand, the Glycerin phantom can reproduce both high- and low-water content organs and is superior to the TX-151 in terms of preservation. Since the Glycerin provides a moisturizing action, there is less evaporation of water from the Glycerin phantom than from the TX-151 phantom. Both phantoms can also maintain their shapes by themselves. This means that a container such a shell is not required. Another feature of these phantoms is that arbitrary shapes can be fabricated using a mold.

Figure 1 shows examples of the frequency dependence of the electrical constants of the TX-151 (○) and the Glycerin (△) phantoms with the characteristics of an average brain (●) [17], where the vertical and horizontal axes represent the conductivity and the relative permittivity of the phantoms, respectively. It is obvious that the frequency characteristic ratio of the conductivity to the relative permittivity for the TX-151 phantom is different from that of the Glycerin phantom. This is due to a difference in the ratio of water content between the Glycerin and TX-151 phantoms, e.g. 60% and 80% in total weight. Furthermore, the ratio of glycerin and water in the Glycerin phantom could be another major factor causing the difference. The frequency characteristics of the TX-151 phantom shown in the figure are very similar to those of the average brain especially above 3 GHz without changing the phantom. Therefore, it is anticipated that the TX-151 phantom can be more readily used and easily adjusted to the target value more so than can the Glycerin phantom at frequencies above 3 GHz. Consequently, we will focus from this point on the TX-151 phantom.

2.2 Adjustment of the Electrical Constants of the TX-151 Phantom

The composition of the TX-151 phantom described in [11],[15] as an example is given in Table 1. Agar is used to maintain the shape of the phantom. In order to mix water with the polyethylene powder (PEP), TX-151 is selected for its sticky property. The amount of TX-151 is adjusted according to the amount of PEP [11]. In addition, the conductivity and permittivity of the phantom are mainly dependent on the concentration of NaCl and PEP, respectively.

As mentioned above, the electrical constants of the TX-151 phantom up to 6.0 GHz are experimentally examined. The target electrical constants, an average brain and muscle [17], and head- and body- equivalent phantoms [18] are selected to adjust the TX-151 phantom constants. The head- and body- equivalent phantoms have been used in the SAR measurement procedure with respect to mobile phones in the US [18]. The adjusted electrical constants at 3.0, 3.8, 5.2, and 5.8 GHz are shown in Fig. 2, where the vertical and horizontal axes represent the conductivity and the relative permittivity of the phantoms, respectively. The frequencies of 5.2 GHz and 5.8 GHz are used for wireless LAN systems and the Industrial Scientific and Medical (ISM) band, respectively. The frequency of 3.8 GHz is the center frequency that is the candidate for allocation to future wireless mobile communications. The target values are also plotted as (×) in the figure. We note that the values of the head- and body-equivalent phantoms are only plotted at 3.0 and 5.8 GHz because those at 3.8 and 5.2 GHz are not defined in [18].

The measuring instrument is an HP-85070B dielectric-probe measurement system (Agilent Technology Company, Palo Alto, CA). Each square in the graph represents the electrical constants for each TX-151 phantom, which are changed based on the amount of PEP and NaCl. The vertical and horizontal dotted lines represent the same amount of PEP or NaCl, respectively.

Table 1  Example composition for TX-151 phantom [11],[15].

<table>
<thead>
<tr>
<th>Ingredient</th>
<th>Amount [g]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deionized water</td>
<td>3375.0</td>
</tr>
<tr>
<td>Agar</td>
<td>104.6</td>
</tr>
<tr>
<td>Sodium chloride (NaCl)</td>
<td>21.5</td>
</tr>
<tr>
<td>Sodium dehydroacetate</td>
<td>2.0</td>
</tr>
<tr>
<td>TX-151</td>
<td>57.1</td>
</tr>
<tr>
<td>Polyethylene powder</td>
<td>548.1</td>
</tr>
</tbody>
</table>

Fig. 1  Examples of frequency dependence of electrical constants of TX-151 and Glycerin phantoms.
The amounts of NaCl and PEP are changed to confirm the range of achievable electrical constants of the phantoms. The amounts of other ingredients except for TX-151 are the same as those in Table 1. In Fig. 2, the electrical constants depend on the amounts of both NaCl and PEP. Conductivity depends on the amounts of both NaCl and PEP while the relative permittivity only relies on PEP. Namely, the electrical constants can be controlled using the following two-steps procedure. First, the amount of PEP is determined for the desired relative permittivity. For example, 675.0 g of PEP is determined for the brain at 3.0 GHz. Second, the conductivity is adjusted by the amount of NaCl, e.g., 20.3 g of NaCl.

2.3 Electrical Constants versus Frequency

The measured electrical constants of four different types of target values (○), i.e., the average brain, average muscle, and the head- and body- equivalent phantoms, versus the frequency from 3.0 to 6.0 GHz are shown in Fig. 3. We note that the values of the head- and body- equivalent phantoms are only plotted at 3.0 and 5.8 GHz because those at 3.8 and 5.2 GHz are not defined in [18]. The error bars show ±5% of the target values. The amounts of PEP, NaCl, and TX-151 for these four types are shown in Table 2 and the others are the same as described in Table 1. In Fig. 3, the electrical constants of the phantoms are almost within ±5% of the target values at each frequency without changing the composition. This means that by using a unique phantom, a broadband frequency that varies between 3.0 GHz to 6.0 GHz can be covered. Moreover, if the amounts of PEP and NaCl are changed, the phantom can be adjusted to different types of

![Diagram](image1.png)

![Diagram](image2.png)

![Diagram](image3.png)

![Diagram](image4.png)

**Fig. 2** Adjustment of the electrical constants of the TX-151 phantoms.

<table>
<thead>
<tr>
<th>Target</th>
<th>PEP [g]</th>
<th>NaCl [g]</th>
<th>TX-151 [g]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average brain</td>
<td>675.0</td>
<td>20.3</td>
<td>45.6</td>
</tr>
<tr>
<td>Average muscle</td>
<td>337.5</td>
<td>10.0</td>
<td>83.3</td>
</tr>
<tr>
<td>Head equivalent</td>
<td>675.0</td>
<td>60.8</td>
<td>45.6</td>
</tr>
<tr>
<td>Body equivalent</td>
<td>337.5</td>
<td>34.1</td>
<td>83.3</td>
</tr>
</tbody>
</table>

**Table 2** Compositions for TX-151 phantom.
2.4 Effect of Electrical Constants of the Phantom

The investigation with respect to the effect by variation of the electrical constants for the phantom is important. It is efficient to know the degree to which the variation will impact the SAR before the measurement when a unique phantom is used for a broadband frequency range. In this study, the effect of the variation is estimated using the FD-TD method, assuming a half-wave dipole antenna and a cubic phantom when the relative permittivity and conductivity of the phantom are changed. Similar studies have already been performed [19], [20]. Kawai et al. investigated in detail the effects of the electrical constants of the phantom at 0.9 and 2.0 GHz. Kang et al. [20] also investigated the effect of conductivity in the 2.45 and 5 GHz bands with a change ratio of 75 and 150% compared to the target value described in [18]. In this paper, both the relative permittivity and conductivity are changed and the peak SAR is calculated at 3.8 and 5.2 GHz considering the usage of a unique phantom for the broadband frequency range. The relative permittivity ($\varepsilon_r$) and the conductivity ($\sigma$) of the phantom at 3.8 GHz and 5.2 GHz are 37.6 and 3.22 S/m, and 36.0 and 4.66 S/m, respectively, which are calculated by a linear interpolation from values taken using a head-equivalent phantom at 3.0 and 5.8 GHz as described by [18].

Table 3 shows the effects of the electrical constants on the peak SAR for both 3.8 and 5.2 GHz. Both the relative permittivity and the conductivity are changed within ±5% because Fig. 3 shows that the electrical constants of each phantom are almost within ±5%. When the relative permittivity is increased, the peak SAR is decreased. On the other hand, when the conductivity is increased, the SAR is also increased. These results are similar to those for 0.9 and 2.0 GHz reported by [19]. However, when the frequency is higher, the effect of the relative permittivity is slightly increased. The worst case variations of the peak SAR at 3.8 and 5.2 GHz are approximately ±6.2% and ±6.6%, respectively, when employing the combination of $\sigma = \pm 5\%$ and $\varepsilon_r = \pm 5\%$. In this paper, although a more detailed investigation with respect to the SAR measurement procedure, e.g., averaging the SAR, is not performed, variations on the 10g-average SAR are introduced briefly. If the 10g-average SAR is evaluated, the worst case variations at 3.8 and 5.2 GHz are reduced to approximately ±1.0% and ±1.5%, respectively.

**Table 3** Effects of electrical constants on peak SAR (Upper: 3.8 GHz, Lower: 5.2 GHz).

<table>
<thead>
<tr>
<th>$\sigma \setminus \varepsilon_r$</th>
<th>$-0.95$</th>
<th>0</th>
<th>1.05</th>
</tr>
</thead>
<tbody>
<tr>
<td>$-0.95$</td>
<td>$-1.50%$</td>
<td>$-3.84$</td>
<td>$-6.10$</td>
</tr>
<tr>
<td></td>
<td>$-0.98$</td>
<td>$-3.82$</td>
<td>$-6.59$</td>
</tr>
<tr>
<td>0</td>
<td>2.40</td>
<td>0</td>
<td>$-2.30$</td>
</tr>
<tr>
<td></td>
<td>2.90</td>
<td>0</td>
<td>$-2.82$</td>
</tr>
<tr>
<td>1.05</td>
<td>6.20</td>
<td>3.74</td>
<td>1.43</td>
</tr>
<tr>
<td></td>
<td>6.65</td>
<td>3.69</td>
<td>0.81</td>
</tr>
</tbody>
</table>
3. Investigation of SAR Measurement Using the Thermographic Method

3.1 Experimental Configuration

The investigation of SAR measurement on the developed phantom using the thermographic method [15] at 5.2 GHz is performed. Calculations using the FD-TD method and the finite difference method based on the heat conduction equation are carried out to investigate the conditions of the thermographic method. The experimental model is illustrated in Fig. 4. A dipole antenna, the length of which is approximately a half-wavelength, is employed as the source of the electromagnetic energy. The antenna is located 10 mm from the phantom surface. The origin of the model directly faces the antenna feeding point and this point is located on the surface of the phantom. Electrical constants of the phantom are calculated by linear interpolation from values taken using a head-equivalent phantom at 3.0 and 5.8 GHz as described in [18]. In other words, the relative permittivity \( \epsilon_r \) and the conductivity \( \sigma \) are 36.0 and 4.66 S/m, respectively.

The measurement is performed in a radio anechoic chamber (Graduate School of Science and Technology, Chiba University, Japan). The SAR experimental configuration is shown in Fig. 5. During the measurement, the forwarded power from the power amplifier and the reflected power from the antenna are monitored.

3.2 Estimation Using the Heat Conduction Equation

When the SAR is measured using the thermographic method, the temperature rise is used directly instead of the electric field shown in Eq. (2).

\[
SAR = c \frac{\Delta T}{\Delta t}
\]  

(2)

where \( c \) is the specific heat \([\text{J/kg·K}]\) of the phantom material, \( \Delta T \) is the temperature rise \([\text{K}]\) at the point, and \( \Delta t \) is the exposure duration \([\text{s}]\). In this equation, it is assumed that thermal diffusion is negligibly small during the experiment. Consequently, this method is basically independent of the frequency. However, if the frequency is higher such as 5.2 GHz, the SAR distributions will be concentrated in a local area more so than if a frequency below 3 GHz is used. This is because the radiating element is physically smaller and the penetration depth is shallower compared to those at a lower frequency. It is anticipated that the effect of thermal diffusion will be greater. Since in Eq. (2) thermal diffusion is approximated as negligibly small during the experiment, the thermal diffusion can influence the SAR.

In order to investigate the thermal diffusion, the heat conduction equation, Eq. (3), and boundary conditions, Eq. (4) [16], are introduced.

\[
\rho c \frac{\partial T}{\partial t} = \kappa \nabla^2 T + \rho \text{SAR}
\]  

(3)

\[
-\kappa \left( \frac{\partial T}{\partial n} \right)_n = h(T_s - T_e)
\]  

(4)

where \( \kappa \) is the thermal conductivity of the phantom \([\text{W/m·K}]\), \( h \) is the heat transfer coefficient \([\text{W/m}^2\cdot\text{K}]\), \( T_s \) is the surface temperature, and \( T_e \) is the external temperature. In this case, the thermal conductivity \( \kappa \) is independent of the location within the phantom. In this study the SAR shown in Eq. (3) is derived from the FD-TD calculation and rise in temperature \( \Delta T \) is evaluated using Eq. (3). The boundary condition, Eq. (4), is adopted at the boundary between the air and the phantom. This condition expresses thermal transfer due to air flow on the surface of the phantom. The finite difference method is used in a numerical calculation for solving Eq. (3) [21]. In the FD-TD method, the cell size in all directions and the time step are 0.5 mm and 0.962 ps, respectively. The Mur’s first order absorbing boundary condition is adopted. For the thermal calculation, the cell size and time step are set to 0.5 mm and 0.2 sec, respectively. The cell arrangement in the thermal calculation is the same as that in the FD-TD method. The initial temperature of the phantom is \( T_e \).

Figure 6 shows the calculated SAR distribution along
Fig. 6  Normalized SAR distributions along z axis at 2.0 and 5.2 GHz calculated by the FD-TD method.

Fig. 7  Calculated and measured temperature rise ($\Delta T$) vs. time at (0.25 mm, 0.25 mm, 0.25 mm).

Fig. 8  Calculated temperature rise ($\Delta T$) difference between $h = \kappa = 0$ and $h = 20 \text{ W/m}^2\cdot\text{K}$ and $\kappa = 0.5 \text{ W/m}\cdot\text{K}$ vs. time.

Fig. 9  Normalized temperature rise ($\Delta T$) distributions at 5.2 GHz.

3.3 Results

The increase in temperature at (0.25 mm, 0.25 mm, 0.25 mm), which is the closest point to the origin, for 5.2 GHz is calculated to estimate the effects of the thermal conductivity ($\kappa$) and the heat transfer coefficient ($h$) (Fig. 7). The thermal conductivity ($\kappa$) is 0.5 W/m·K and the heat capacity ($c$) is 3,700 J/kg·K (measured by Agne Gijutsu Center Co., Ltd., Tokyo, Japan). The heat transfer coefficient ($h$) is 20.0 W/m$^2$·K, which is normally used in the estimation, and density ($\rho$) is 870 kg/m$^3$. The antenna input power is 9.68 W. In this estimation, the thermal conductivity $\kappa = 0$ and 0.1 W/m·K and the heat transfer coefficient $h = 0$ is considered for the comparison. The expression $h = \kappa = 0$ means that no thermal diffusion is considered. As a result, if $h = 20 \text{ W/m}^2\cdot\text{K}$ and $\kappa = 0.5 \text{ W/m}\cdot\text{K}$, which is a realistic case, the rise in temperature becomes less prominent compared to $h = \kappa = 0$. In addition, there is no significant change between $h = 0$ and $\kappa = 0.5 \text{ W/m}\cdot\text{K}$. However, the results for $h = 20 \text{ W/m}^2\cdot\text{K}$ and $\kappa = 0.1 \text{ W/m}\cdot\text{K}$ exhibit a difference compared to $h = 20 \text{ W/m}^2\cdot\text{K}$ and $\kappa = 0.5 \text{ W/m}\cdot\text{K}$. This means that the thermal conductivity inside the phantom influences the temperature rise in this frequency range compared to heat convection from the surface over a short period.

The measured results and those calculated using the heat conduction equation agree fairly well, indicating that the thermal diffusion is well simulated in the calculation. As shown in the figure, both the measured and calculated temperature-rise curves are suppressed when $\kappa$ is considered and the exposure duration is increased. After approximately 2 sec, the effects of thermal diffusion appear due to thermal conductivity. Figure 8 shows the difference in the temperature increase (%) between $h = \kappa = 0$ and $h = 20 \text{ W/m}^2\cdot\text{K}$ and $\kappa = 0.5 \text{ W/m}\cdot\text{K}$ at both 2.0 and 5.2 GHz. It appears that temperature increase at 2.0 GHz is suppressed as well. However, the suppression at 5.2 GHz is larger than that at 2.0 GHz as mentioned above.

Figure 9 shows the measured and calculated tempera-
ture rise distributions along the z-axis at 5.2 GHz for 2 and 15 sec, which are normalized to the calculated maximum temperature rise for $h = \kappa = 0$ for each time, respectively. The measured and calculated temperature rise distributions are in fairly good agreement even though there is variation in the measurement. Figure 10 also shows the calculated temperature rise distributions along the x-axis. As discussed above, when the exposure duration is increased, the temperature rise is lower than that for $h = \kappa = 0$ due to thermal diffusion. It is expected that the estimated SAR from the temperature rise after 2 sec will be mostly within $\pm 10\%$. However, there is a comparatively large variation in the measured values. This is due to the temperature resolution of the thermographic camera used to measure the temperature rise. On the other hand, in the case of 15 sec the estimated SAR is lower than that for 2 sec. The variation in the measurement, however, is smaller because the effect of the resolution is relatively small. As a result, although the thermographic method is independent of the frequency, the exposure duration time must be taken into account in the higher frequency range because the thermal diffusion cannot be neglected. If a thermographic camera with a higher temperature resolution is used and the temperature rise is measured during a very short time such as 1 sec, it is possible to derive the SAR without the influence of thermal diffusion.

4. Conclusions

In this paper, the electrical constants of the biological tissue-equivalent agar-based solid phantoms from 3.0 to 6.0 GHz were described. The developed phantoms can reproduce the electrical constants of the biological tissues from 3.0 to 6.0 GHz, and it is not necessary to change the phantom for each frequency band in the range of 3.0 to 6.0 GHz during the measurements. Moreover, the adjustments of the dielectric constants of the phantom at 3.0, 3.8, 5.2, and 5.8 GHz were presented. The constants of this phantom can be adjusted mainly using PEP and NaCl. The phantom can be used to evaluate the SAR as well as the antenna characteristics in the range of 3.0 to 6.0 GHz for research and development in particular.

The effect on the variation of the electrical constants was investigated at 3.8 and 5.2 GHz using the FD-TD method. The maximum variations on the peak SAR at 3.8 and 5.2 GHz were approximately $\pm 6.2\%$ and $\pm 6.6\%$, respectively, when the combination of $\sigma = \pm 5\%$ and $\epsilon_r = \pm 5\%$ was considered. However, if the SAR is evaluated based on the average volume, i.e., the 10g-average SAR, the worst case variations at 3.8 and 5.2 GHz are reduced to approximately $\pm 1.0\%$ and $\pm 1.5\%$, respectively. These results can also be applied to the SAR measurement in liquid.

We investigated the SAR measurement at 5.2 GHz using the thermographic method on the developed phantom. Calculations using the FD-TD method and the finite difference method based on the heat conduction equation were carried out in order to evaluate the thermal diffusion in the measurement using the thermographic method. The measured and calculated results were in good agreement. There is evidence that the thermal diffusion influences the SAR estimation at 5.2 GHz more than in a lower frequency range even though this method basically does not depend on the frequency. Therefore, consideration of the influence of the thermal diffusion on the thermographic method at a higher frequency is important.

References

quantity of heat from the surface is much less than that from the SAR at 2 and 15 sec. However, at 240 sec the quantity of heat from the surface becomes approximately the same as that from the SAR. This indicates that the effect of “h” is not the main role for thermal diffusion during a very short time. In fact, at 240 sec the gradient of thermal distribution normal to the surface is negative though the gradient is positive at 2 and 15 sec (Fig. 10). This means that the direction of heat flux is toward the outside at 240 sec.

Table A-1  Heat flux from the surface versus time.

<table>
<thead>
<tr>
<th>Time</th>
<th>Heat flux [W/m²]</th>
<th>Quantity of heat [W]</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 sec</td>
<td>19.54</td>
<td>4.89×10⁻⁶</td>
</tr>
<tr>
<td>15 sec</td>
<td>114.2</td>
<td>2.86×10⁻⁵</td>
</tr>
<tr>
<td>240 sec</td>
<td>610.6</td>
<td>1.53×10⁻⁴</td>
</tr>
</tbody>
</table>

Appendix: Consideration of Thermal Diffusion

The effects of thermal conductivity inside the phantom and heat convection from the surface are investigated in this appendix. Figure 7 already indicated that the effect of thermal conductivity inside the phantom is greater than that of heat convection from the surface during a 15 sec period. Equation (A-1) is called Newton’s Law of Cooling, which explains heat convection (the heat flux [W/m²]) from the surface. This equation is the same as the right part of Eq. (4).

\[ q = h(T_S - T_E) \]  

(A-1)

where \( q \) is the heat flux [W/m²] in terms of the normal direction to the surface, meaning mobility of heat quantity.

In order to estimate the effect of \( h \) quantitatively, \( q \) is calculated using Eq. (A-1) at 2 and 15 sec (Table A-1). In addition, \( q \) at 240 sec is calculated for comparison. Since in the thermal calculation the cell size is 0.5 mm, the quantity of heat is obtained by the heat flux \( \times \) the cell size (0.5 square mm). It is clear that the quantity of heat from the surface increases, as time elapses. On the other hand, the quantity of heat based on the SAR in the volume of 0.5 mm³, which is independent of time elapse, is 2.16×10⁻⁴ W. The
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