Magnetic Field Homogeneity of Birdcage Coil for 4 T MRI System with No Lumped Circuit Elements

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SUMMARY In recent years, magnetic resonance imaging (MRI) systems that operate up to under 3 T are being used in clinical practice in Japan. In order to achieve the requirements of higher image quality and shorter imaging times, devices that utilize high magnetic fields (> 3 T) and high power electromagnetic (EM) wave pulses have been developed. The rise of the static magnetic field is proportional to the increase of the EM wave frequency which raises the issue of variation in capacitance used in the radio frequency (RF) coil for MRI system. In addition, increasing power causes problems of withstanding voltage and these approaches leads to generation of non-uniform magnetic field inside the RF coil. Therefore, we proposed a birdcage coil without the use of lumped circuit elements for MRI systems in previous study. However, it is difficult to fabricate this birdcage coil. Hence, simply-structured birdcage coil with no lumped circuit elements is desired. In this paper, we propose a simply-structured birdcage coil with no lumped circuit elements for a 4 T MRI system. In addition, the authors investigated the input impedance and magnetic field distribution of the proposed coil by FDTD calculations and measurements. The results confirm that the proposed birdcage coil matches the performance of the conventional birdcage coil which includes several capacitors.

key words: magnetic resonance imaging (MRI), birdcage coil, finite-difference time-domain (FDTD) method, biological tissue-equivalent phantom

1. Introduction

Magnetic resonance imaging (MRI) is being widely used to obtain clear images inside the human body, especially of high water content tissues. The fundamental principle of MR imaging is to receive nuclear magnetic resonance (NMR) signals induced by irradiating the human body placed inside a strong static magnetic field with electromagnetic (EM) wave pulses. The MRI system is composed of various elements including a radio frequency (RF) coil, which plays an essential role in imaging [1]. Several types of RF coils, such as birdcage coils, saddle coils, surface coils, transverse electromagnetic (TEM) coils etc. have been developed and used depending on the body part to be imaged [1]–[4]. These RF coils operate as an antenna that “irradiates the body with EM wave pulses in order to generate NMR signals” and “receiving the NMR signals emitted from the body”. This paper focuses on the birdcage coil, which is the most popular type of volume coil. Frequency to emit the NMR signal depends on nucleus properties in human body. It is necessary to use an EM wave in certain specified frequency to emit the NMR signal. Here, frequency of EM fields, \(f\) [Hz] is given by the following equation.

\[
f = \frac{\gamma \cdot B}{2\pi}
\]

where \(f\) is the Lamor precession or resonant frequency of the nucleus [Hz], \(\gamma\) is the gyromagnetic ratio of nuclear [Hz/T]. In the case of water composed of hydrogen atoms, \(\gamma = 42.6\,\text{MHz/T}\). Additionally, \(B\) is the magnitude of the static magnetic flux density [T]. In this paper, the authors describe magnetic flux density as magnetic field for reasons of expediency. Thus, frequency to emit NMR signal is directly proportional to the strength of the static magnetic field.

Recent MRI systems that operate at up to 3 T are being used in clinical practice in Japan [5]. In order to achieve the requirement of obtaining more high-quality images and short imaging time, devices, which utilize high magnetic field (> 3 T) and high power EM wave pulses, have been developed [6], [7]. However, some problems caused by high magnetic field and high power EM wave pulses. For instance, the increase of static magnetic field strength causes a rise in the frequency of EM pulses. In such a case, small variability of capacitances used in the birdcage coil, which is one of the most-used volume coils and is loaded a lot of uniform capacitances, will not be ignored. In addition, the use of high power EM pulses will induce breakdown of the capacitances. The improvement of the above problems would increase costs for manufacturing of the coil. It is predicted that these problems are going to become increasingly serious problems when high magnetic field (> 3 T) is utilized with devices for the MRI system. Hence, if we can develop the birdcage coil for MRI system with no lumped circuit elements such as capacitance, it is extremely useful. For this reason, we have developed birdcage coil for MRI system with no lumped circuit element [8]. This birdcage coil has circular conductors which are two different diameters. These conductors were constructed on both surfaces of dielectric cylinder. In this way, this birdcage coil can generate capacitance between circular conductors which are two different diameters. Due to this, birdcage coil does not need any capacitors as lumped circuit elements. However, if conductors on dielectric cylinder are out of position during process of manufacture, characteristics of this birdcage coil become depleted because capacitance changes between some
conductors on both surfaces of dielectric cylinder. In other words, it is difficult to fabricate this birdcage coil. Therefore, simply-structured birdcage coil with no lumped circuit elements to reduce manufacturing error is desired.

In this paper, we proposed the simply-structured birdcage coil with no lumped circuit elements to reduce manufacturing error. To be more specific, conductors of the birdcage coil with no lumped circuit elements were constructed on single side surface of dielectric cylinder. It is considered that proposed birdcage coil can be manufactured by technique of making a single side printed circuit board.

2. Calculation Model

2.1 Head Model

Figure 1 show the head model used in the numerical calculation and the experiment. This model is 180 mm in diameter, 250 mm in length and is made of a uniform medium of an average brain tissue [9]. The composition of the phantom for experiment is listed in Table 1. The target values of electrical properties of the phantom are $\varepsilon_r = 58.2$ and $\sigma = 0.49 \, S/m$ at 170 MHz [10]. At 170 MHz, the errors between the target values and the measured electrical constants are 3.4% and 4.1% for relative permittivity $\varepsilon_r$ and conductivity $\sigma$, respectively. Thus, there is no influence on the birdcage coil performances with such differences.

2.2 Structure of the Birdcage Coil

The RF coil employed in this paper is a birdcage coil for 4 T MRI system. From the Eq. (1), operating frequency of the coil is approximately 170 MHz. Figure 2(a) shows structure of the proposed birdcage coil, previous birdcage coil with no lumped circuit element in Ref. [8] is shown Fig. 2(b) and the conventional birdcage coil is shown Fig. 2(c) for comparison, respectively. Figure 3 shows sectional view of two birdcage coils. The birdcage coil consists of two circular conductors and some conductors which make a connection with circular conductors. The former is called end-ring and the latter is called element. Here, both coils consist of sixteen elements.

Moreover, in order to generate a homogenous magnetic field inside the birdcage coil and control the resonance frequency of the conventional birdcage coil to approximately 170 MHz, a total of thirty two capacitors were attached to the both end-rings of the conventional birdcage coil such as Fig. 2(c). Resonance frequency of the birdcage coil is varied according to the capacitance. In addition, magnetic field distribution inside the coil is varied according to current pattern on elements. For example, to create a homogeneous magnetic field inside cylindrical birdcage coils, the current pattern on a conducting surface should have a sinusoidal dependence on the azimuthal angle of the element location. Please see Ref. [1] for more information about operating principle of the birdcage coil. In this paper, all capacitors have 14.4pF based on an analysis of Birdcage Builder [11] which is computer program provided by Pennsylvania State University. The Birdcage Builder can be used to calculate the current pattern on a conducting surface of element location, and the necessary capacitances of the birdcage coil of a given geometry (diameter of birdcage coil, number of elements, required resonant frequency, and so on) by performing lumped circuit analysis using virtual ground assumptions. In capacitance calculation, each end-ring was treated as a number of segments located between the elements, and the required capacitances were calculated as follows: (1) calculate the current intensity in the leg following the desired current distribution (for example, it will be a sinusoidal distribution in a circular coil design) according to elements angular position, (2) calculate current intensity in the end-ring segments

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Table 1 Composition of phantom.
by Kirchhoff’s law, (3) calculate the effective inductance of legs concerning the effect of RF shield, (4) calculate the effective inductance of end-ring segments, and (5) calculate the capacitance by performing lumped circuit analysis using Kirchhoff’s law. For example, a circuit model for birdcage coil design is shown in Fig. 4. The $L_{\text{eff}}$ and $L_{\text{ER}}$ are the effective inductance of the element and end-ring segment, $C$ is the capacitor inserted on the end-ring segment, $I$ is the current intensity in the end-ring segment, and $n$ is the index.

Figure 2(a) is the proposed birdcage coil without the use of lumped circuit elements. In order to control the resonance frequency of the proposed birdcage coil, gaps are used instead some capacitors such as Fig. 2(a). Therefore, this birdcage coil does not need the capacitor that is the lumped circuit elements. Structure of the proposed birdcage coil is simpler than the coil in Ref. [8] because conductor of Ref. [8] was constructed on both surfaces of dielectric cylinder. Here, end-rings and sixteen elements were constructed on the dielectric pipe ($\varepsilon_r = 2.1$), whose pipe wall thickness is 3 mm.

In this paper, two coils and RF shield are same in size such as Fig. 3(a) and (b). The diameter and the length of both coils are 300 mm and 330 mm each, which is sufficiently large for the head model to be set inside. Additionally, both coils are enclosed in a cylindrical RF shield. The diameter and the length of the RF shield are 400 mm and 440 mm, respectively. All these are composed of metallic sheets. Dimensions of coil and the cylindrical RF shield were determined by Refs. [9], [12], and [13]. In addition, two feeding points were employed in these calculations and the phase difference between them is 90 degree. This excitation method is called “quadrature excitation” and can generate uniform rotate magnetic field inside the birdcage coil.
grid FDTD algorithm was adopted. The absorbing boundary condition is 8 layers of Perfectly Matched Layer (PML).

3. Input Impedance of the Proposed Coil

In this paper, in order to adjust the resonant frequency, widths of gaps between end-rings \( g \) (see Fig. 2(a)) are changed. Other parameters (e.g. overlap-length between three end-rings, distance between element and center end-ring, and so on) are maintained constant. Figure 6 show relationships between resonant frequency and \( g \). In this paper, impedance-matching of the birdcage coil is not considered because MRI system usually has matching circuit (i.e. we consider only adjust the resonant frequency of the coil.). Moreover, birdcage coil is considered as a parallel resonant circuit as shown in Fig. 4. Generally, a parallel resonant circuit has high impedance at resonant frequency. In other words, absolute value of impedance has local maximum value at resonant frequency. Therefore, absolute value of impedance is shown in this paper because it is only necessary to adjust the resonant frequency. As a result, the resonance frequency was confirmed to be approximately 170 MHz, when widths of gaps are 0.2 mm. Thus, it is considered that proposed coil when widths of gaps are 0.2 mm and conventional coil which are loaded with capacitance of 14.4 pF are equivalent.

In order to compare the measured and calculated input impedances of the proposed birdcage coil containing the head model, when widths of gaps are 0.2 mm are shown in Fig. 7. The continuous line is the calculated result and the broken line is the measured result. The input impedance was calculated at the feeding point at \( \phi = 0^\circ \), same as the measured. Here, the measuring instrument was N5230C PNA-L network analyzer by the Agilent Technologies, Santa Clara, California.

As a result, the resonance frequency is confirmed to be approximately 170 MHz. However, slight shifts in resonant frequency and absolute value of impedance between the measured and calculated results were confirmed. These shifts attributed to fabrication error in, such as, the dimension of gaps.

4. Magnetic Field Distribution

It is considered that magnetic field homogeneity in the center of the coil is important because the coil is placed in such a way that target organ is positioned roughly in the center of the coil. In addition, the direction of rotation of the nuclear is radial direction of the coil (i.e. \( x-y \) plane). Thus, it is necessary to generate rotate magnetic field in \( x-y \) plane. For these reasons, this paper describes the results of magnetic field distributions in \( x-y \) plane.

4.1 Calculated Magnetic Field Distribution

Figure 8(a) shows the magnetic field distribution of the proposed coil containing the head model in the \( x-y \) plane at center of the coil (\( z = 0 \) mm). In addition, the magnetic field distribution of the conventional coil containing the head model is shown in Fig. 8(b) for comparison. Here, the magnetic field levels of proposed coil and conventional coil were normalized with equal input power. From these results, it was confirmed that both coils generate uniform magnetic field inside the head model. Figure 9 shows the profiles of magnetic field. The observation line is \( x \) axis at \( y = 0 \) mm in Fig. 8. The continuous line is the result of proposed coil and the broken line is the result of conventional coil. As a result, it was confirmed that the proposed coil has an equivalent uniformity to the conventional birdcage coil. In addition, each component (\( H_x \), \( H_y \) and \( H_z \)) of magnetic field distributions inside the proposed coil containing the head model is shown in Fig. 10. From these results, we confirmed that level of \( H_z \) component, which is parallel to the axial direction of the coil, was small in comparison with the levels of \( H_x \) and \( H_y \) components. Thus, the spatial phase difference of 90 degrees caused by quadrature excitation between \( H_x \) and \( H_y \) components of magnetic field distributions were observed. These distributions were observed for a similar result in conventional birdcage coil and it is non-unique characteristics of proposed coil. From these results, it is suggested that the proposed birdcage coil can
use for MR imaging. Additionally, in order to compare the magnetic field uniformity inside the head, average variation of the magnetic field inside a head model were calculated by applying the following Eq. (1). The average variation is defined as

\[ \delta_{\text{ave}} = \frac{1}{S} \int_{S} |H - H_{\text{ave}}| \, ds \]  

where \( S \) denotes the circular region [m²], and \( H_{\text{ave}} \) denotes average value of \( H \) over the region. In this case, \( S \) is cross section of the phantom. In addition, range of \( H_{\text{ave}} \) as defined from 0 to 1. Table 3 illustrates the average variations of magnetic field in the head model for the proposed coil and the conventional coil. The average variation of the proposed coil is approximately \( \delta_{\text{ave}} = 0.147 \), the average variation of the conventional coil is the \( \delta_{\text{ave}} = 0.158 \). As a result, average variation of the conventional coil is slightly larger than the average variation of the proposed coil. However, error of the average variation between the conventional coil and proposed coil was negligible small in terms of practice. Accordingly, it is considered that the proposed birdcage coil has an equivalent homogeneity of magnetic field to the conventional birdcage coil.

### Table 3  Comparison of the average variation \( \delta_{\text{ave}} \).

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4.2 Measurement of the Magnetic Field Distribution

Here, we describe the measurement of the magnetic field distribution inside the human head model and thereby validate the calculated results. Figure 11 shows the experimental setup, where the arrangement of the birdcage coil and human head model is the same as that in Fig. 5. Here, gel phantom is used as a human head model. Gel phantom is filled in dielectric pipe (\( \varepsilon_r = 2.1 \)) and thickness of dielectric pipe is 3 mm. The composition of the gel phantom for measurement of magnetic field distribution is listed.
in Table 4. At 170 MHz, the errors between the target values of electrical properties of the gel phantom and the measured electrical constants are less or equal 10% for relative permittivity $\varepsilon_r$ and conductivity $\sigma$, respectively. Here, the signal was excited at the position $\phi = 0^\circ$ in Fig. 5. The proposed birdcage coil has rotationally-symmetrical structure and equal amplitude signals were exited at two feeding points. From this reason, in the case of 1-port, obtained magnetic field becomes rotation symmetry. Therefore, magnetic field was measured by using 1-port feeding. In order to feed the proposed birdcage coil, a signal generator (8657B Hewlett Packard, Palo Alto, California) and a power amplifier (LA100UF-CE Kalmus, Bothell, Washington) were used. The shielded loop probe was used as the magnetic field probe. Diameter of a shielded loop probe is 5 mm. Then, $H_x$ and $H_y$ were measured by orienting the probe antenna along the $x$ axis at $y = 0$ mm in Fig. 8. Here, the $H_z$ component is omitted because its level is very low as compared to $H_x$ and $H_y$. A spectrum analyzer (Agilent E4403B) was used to measure the received signal level. The scanning interval on the line was 10 mm. Figure 12 compares the measured and calculated magnetic field distribution on the observation line $(q = z = 0$ mm, $-70 \leq x \leq 70$ mm). The levels are normalized with the maximum value on the observation lines in both cases. The continuous line is the calculated result and square symbols are the measured result. As a result, we confirmed that measurement result disagree with the calculation result in the range of $-70$ mm $\leq x \leq -50$ mm because the range is noise floor of the spectrum analyzer. However, good agreement was observed between the measured and numerical calculated results of the magnetic field level in the range of $|x| < 50$ mm.

5. Conclusions

This paper proposes a birdcage coil with no lumped circuit elements for 4 T MRI systems; it is an enhanced version of our previous proposal. Conductor of previous birdcage coil was constructed on both surfaces of dielectric cylinder. On the one hand, conductor of proposed birdcage coil was constructed on only one side. Firstly, the authors have clarified the input impedance of the proposed coil by use of FDTD calculations and measurements. The results show that the resonance frequency was approximately 170 MHz, the operating frequency of a 4 T MRI system. Moreover, good agreement was observed between the measured and calculated input impedances.

Secondly, the magnetic field distributions of proposed birdcage coil were investigated. As a result, it was confirmed that the proposed birdcage coil matches the uniformity of the conventional birdcage coil.

Finally, we described the measurement of the magnetic field distribution inside the human head model and thereby validate the numerical calculated results. Good agreement was observed between the measured and calculated results.

The future challenge is to investigate the magnetic field distribution inside a realistic human head model by use of FDTD calculations.

References


### Table 4 Composition of gel phantom.

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**Fig. 12** The measured and calculated magnetic field distribution on the observation line at the position $\phi = 90^\circ$. 

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